

Výrazy

- operace se zlomky
- vzorce
- rozklad na součin
- užití rozkladu kvadratického trojčlenu
- částečné odmocňování
- usměrňování zlomků
- mocniny a odmocniny

operace se zlomky

podmínky!

sčítání, odčítání – společný jmenovatel

$$\frac{x}{x+3} + \frac{1}{x} + 2$$

$$\frac{1}{x-2} - \frac{4-x}{x^2-2x}$$

$$\frac{a-1}{a^2+a} - \frac{a-3}{a^2-1} - \frac{a+2}{2a^2+2a}$$

násobení, dělení

$$\frac{x}{x+3} * \frac{x^2-9}{3yx}$$

$$\frac{x^2}{x-2} * \frac{4-2x}{x^2-2x}$$

$$\frac{2x^2-2xy}{ab^2} \div \frac{4x^2-4y^2}{6a^2b}$$

$$\frac{\frac{1}{x} + \frac{1}{y}}{\frac{x+y}{xy}}$$

$$\left[\left(\frac{x-y}{y-x} \right) \div \left(\frac{x}{y} + \frac{y}{x} - 2 \right) \right] \div \left(1 + \frac{y}{x} \right)$$

$$\left(b + \frac{a-b}{1+ab} \right) \div \left(1 - \frac{b(a-b)}{1+ab} \right)$$

$$(x^3 - x^2 - x - 15) \div (x - 3)$$

$$(2x^3 + 3x^2 + x + 6) \div (x + 2) = 2x^2 - x + 3$$

$$(8x^4 - 16x^3 + 8x^2 - 7x + 6) \div (2x - 3) = 4x^3 - 2x^2 + x - 2$$

vzorce

$$(a \pm b)^2 = a^2 \pm 2ab + b^2$$

$$(a \pm b)^3 = a^3 \pm 3a^2b + 3ab^2 \pm b^3$$

$$a^2 - b^2 = (a - b)(a + b)$$

$$a^2 + b^2 = \text{toto není vzorec}$$

$$a^3 - b^3 = (a - b)(a^2 + ab + b^2)$$

$$a^3 + b^3 = (a + b)(a^2 - ab + b^2)$$

$$\frac{\left(\frac{x}{y} + \frac{y}{x} + 1\right) \left(\frac{1}{x} - \frac{1}{y}\right)^2}{\frac{x^2}{y^2} + \frac{y^2}{x^2} - \left(\frac{x}{y} + \frac{y}{x}\right)}$$

$$\frac{m^4 - n^4}{m^2 - 2mn + n^2} * \frac{m - n}{m^2 + mn}$$

$$\left(\frac{4x^3}{x^3 - y^3} \div \frac{2x^3}{x^2 - 2xy + y^2}\right) \cdot \frac{x^2 + xy + y^2}{x^2 - y^2}$$

$$\left(\frac{a+b}{2a-2b} - \frac{a-b}{2a+2b} - \frac{2b^2}{b^2-a^2}\right) \cdot \left(\frac{1}{b} - \frac{1}{a}\right) = \frac{2}{a}$$

rozklad na součin

- vytýkání
- vzorce
- dvojice

$$27x^3 - 8y^3$$

$$2x^3 - 12x^2y^2 + 24xy^4 - 16y^6$$

$$x^2 - xy - 2x + 2y$$

$$\frac{(a+b)^2 - (c+d)^2}{(a+c)^2 - (b+d)^2}$$

$$\frac{x^3 - 125}{x^3 - 15x^2 + 75x - 125}$$

$$\frac{x - xy + z - zy}{1 - 3y + 3y^3 - y^2}$$

$$\frac{x^3 - 2x^2 - x + 2}{x^3 + 2x^2 - x - 2}$$

$$\frac{x^3 - 3x^2 - x + 3}{x^3 - 2x^2 - 3x} = \frac{x-1}{x}$$

užití rozkladu kvadratického trojčlenu

Součinnový tvar a Vietovy vzorce:

$$ax^2 + bx + c = 0$$

$$a(x-r)(x-s) = 0$$

$$r+s = -\frac{b}{a} \quad r \cdot s = \frac{c}{a}$$

$$x^2 - 2x - 3$$

$$x^2 - 5x + 6$$

$$x^2 - 2x - 8$$

$$x^2 + 7x + 10$$

$$x^2 - x - 6$$

$$x^2 + x - 56$$

$$3x^2 - 18x + 15$$

$$\left[\frac{4x}{x^2 + 4} \cdot \left(\frac{2}{x^2 - 2x} - \frac{x}{4 - 2x} \right) - \frac{4}{x^2 - 4} \right] : \frac{x}{x-2}$$

mocniny a odmocniny

pravidla:

$a^0 = 1$	$\sqrt[n]{a} \cdot \sqrt[n]{b} = \sqrt[n]{ab}$
$a^{-n} = \frac{1}{a^n}$	$\frac{\sqrt[n]{a}}{\sqrt[n]{b}} = \sqrt[n]{\frac{a}{b}}$
$a^{\frac{r}{s}} = \sqrt[s]{a^r}$	$\sqrt[m]{\sqrt[n]{a}} = \sqrt[mn]{a}$
$a^r \cdot a^s = a^{r+s}$	$(\sqrt[n]{a})^s = \sqrt[n]{a^s}$
$(a^r)^s = a^{r \cdot s}$	$\sqrt[n]{a} = \sqrt[np]{a^p}$
$(a \cdot b)^r = a^r \cdot b^r$	$\sqrt[kn]{a^{km}} = \sqrt[n]{a^m}$
$\left(\frac{a}{b}\right)^r = \frac{a^r}{b^r}$	
$a^r : a^s = a^{r-s}$	

částečné odmocňování

$$\sqrt{120} = \sqrt{4 \cdot 30} = \sqrt{4} \cdot \sqrt{30} = 2\sqrt{30}$$

$$\sqrt{200}$$

$$\sqrt{150}$$

$$\sqrt{1000}$$

$$\sqrt[3]{108}$$

$$\sqrt[3]{128}$$

$$\sqrt[3]{x^5 y^3 z^7}$$

$$(2\sqrt{3} + \sqrt{5})^2 - 2\sqrt{60} - 17 = 0$$

$$(3 - 2\sqrt{2})^2 - (-1 + 3\sqrt{2}) \cdot \sqrt{8} = 5 - 10\sqrt{2}$$

$$5\sqrt{20} - 3\sqrt{125} + 7\sqrt{45} + \sqrt{180} = 22\sqrt{5}$$

usměrňování zlomků

$$\frac{2}{\sqrt{3}} = \frac{2}{\sqrt{3}} \cdot \frac{\sqrt{3}}{\sqrt{3}} = \frac{2\sqrt{3}}{3}$$

$$\frac{2}{\sqrt{2}-\sqrt{5}} = \frac{2}{\sqrt{2}-\sqrt{5}} \cdot \frac{\sqrt{2}+\sqrt{5}}{\sqrt{2}+\sqrt{5}} = \frac{2\sqrt{2}+2\sqrt{5}}{2-5} = \frac{2\sqrt{2}+2\sqrt{5}}{-3}$$

$$\frac{2\sqrt{3}}{\sqrt{2}-3} = \frac{2\sqrt{3}}{\sqrt{2}-3} \cdot \frac{\sqrt{2}-3}{\sqrt{2}-3} = \frac{2\sqrt{6}-6\sqrt{3}}{2-9} = \frac{2\sqrt{6}-6\sqrt{3}}{-7}$$

$$\frac{2}{\sqrt{3}-\sqrt{4}}$$

$$\frac{ab}{3\sqrt{a^3b}}$$

$$\frac{\sqrt{ab}-a\sqrt{b}}{\sqrt{ab}}$$

$$\frac{2\sqrt{x}-\sqrt{2x}}{\sqrt{x}-\sqrt{2}}$$

$$\frac{\sqrt{2}-\sqrt{3}}{1-\sqrt{2}} + \frac{\sqrt{6}+\sqrt{2}}{\sqrt{3}-1} = \sqrt{2} + \sqrt{3} + 2\sqrt{6} - 2$$

Upravte:

a) $(3 - 2\sqrt{2})^2 - (-1 + 3\sqrt{2})\sqrt{8}$ [$5 - 10\sqrt{2}$]

b) $(2\sqrt{3} + \sqrt{5})^2 - 2\sqrt{60} - 17$ [0]

c) $\left(\frac{1+\sqrt{2}}{\sqrt{2}} - \frac{\sqrt{2}}{1-\sqrt{2}}\right)^2$ [$\frac{9(3+2\sqrt{2})}{2}$]

d) $\left(\frac{3-2\sqrt{2}}{3\sqrt{2}-4}\right)^2$ [$\frac{1}{2}$]

e) $f(a, b) = \left[a^{-\frac{3}{2}} b (ab^{-2})^{-\frac{1}{2}} (a^{-1})^{-\frac{2}{3}} \right]^3$ Vypočítejte: $f\left(\frac{\sqrt{2}}{2}, \frac{1}{\sqrt{2}}\right)$ [1]

Zjednodušte:

a) $\frac{28a^{-3}b^4d^{-5}}{64ab^6c^{-2}} : \frac{7a^3b^{-2}c}{8a^2d^3}$ b) $(x \cdot x^{\frac{1}{3}})^{\frac{1}{2}} \cdot (x \cdot x^{\frac{1}{2}})^{\frac{1}{3}}$

$$\sqrt[5]{\frac{4}{\sqrt[3]{2}}} \div \sqrt[3]{\frac{2}{\sqrt[5]{8}}} = \sqrt[5]{2}$$

$$\frac{\left(10^{\frac{1}{3}} \cdot 8^{\frac{1}{2}}\right)^{-3}}{\left(5^{\frac{1}{4}} \cdot 4^{\frac{1}{8}}\right)^2} \div \frac{\sqrt{2\sqrt[3]{4}}}{\sqrt[3]{2\sqrt[4]{4}}} = \frac{4\sqrt[3]{4}\sqrt{5}}{25}$$

$$\frac{\sqrt[3]{\sqrt{a} \cdot a}}{\sqrt[3]{\left(\sqrt{a} \cdot \frac{1}{a^2}\right)^2}} = a\sqrt[3]{a^2}$$

$$\left[(a^{0,5} + b^{0,5})^2 - \left(\frac{\sqrt{a} - \sqrt{b}}{a^{1,5} - b^{1,5}} \right)^{-1} \right] \cdot (ab)^{-0,5}$$

$$1 + \frac{(4 - a^2)^{-\frac{1}{2}} - (2 - a)^{-\frac{1}{2}}}{(2 + a)^{-\frac{1}{2}} - (4 - a^2)^{-\frac{1}{2}}} \cdot \frac{1 - a}{1 - \sqrt{2 - a}}$$

$$\left(\frac{x^{-2} - x^{-4}}{x^{-2} - 1} \right) : \left(\frac{1 - x^{-\frac{1}{2}}}{x^{-\frac{1}{2}} - x^{-1}} \right)$$

Zjednodušte výrazy a výsledek zapište ve tvaru odmocniny:

a) $\left(\frac{a\sqrt{a+b\sqrt{b}}}{\sqrt{a+\sqrt{b}}} - \sqrt{ab} \right) : (a-b) + \frac{2\sqrt{b}}{\sqrt{a+\sqrt{b}}}$ $[1; a \geq 0 \wedge b \geq 0 \wedge a \neq b]$

b) $\sqrt{a\sqrt[3]{b-1}} : \sqrt[3]{b^2\sqrt{a}} + \sqrt[6]{b} : b$, $\left[\frac{1+\sqrt[3]{a}}{\sqrt[6]{b^5}}; a > 0 \wedge b > 0 \right]$

c) $\sqrt[4]{a^3} \cdot \sqrt[3]{a^2} \cdot \sqrt{a}$, $\left[\sqrt[12]{a^{23}}; a \geq 0 \right]$

d) $\sqrt{x\sqrt[3]{x}} \cdot \sqrt[3]{x\sqrt{x}}$, $\left[\sqrt[6]{x^7}; x \geq 0 \right]$

e) $\sqrt[5]{\left(\frac{\sqrt{m \cdot m^{-2}}}{m^{\frac{1}{3}}} \right)^{-2}}$, $\left[\sqrt[15]{m^{11}}; m > 0 \right]$

f) $\frac{\sqrt[3]{a^{-2}\sqrt{a^3}}}{\sqrt[3]{\sqrt{a^4}\sqrt{a^{-3}}}}$, $\left[\sqrt[3]{a^5}; a > 0 \right]$

g) $\sqrt{ab} \cdot \sqrt[3]{4a^2b^4} \cdot \sqrt[4]{8a^3b^7} \cdot \sqrt[12]{2a^3b^9}$, $\left[\sqrt[23]{2^3 \cdot a^{13} b^{26}}; a \geq 0 \wedge b \geq 0 \right]$

h) $\sqrt{\frac{a}{b}} \sqrt[3]{\frac{a^2}{b^2}} \sqrt[4]{\frac{a^3}{b^3}}$, $\left[\sqrt[24]{\left(\frac{a}{b}\right)^{29}}; a \geq 0 \wedge b > 0 \right]$